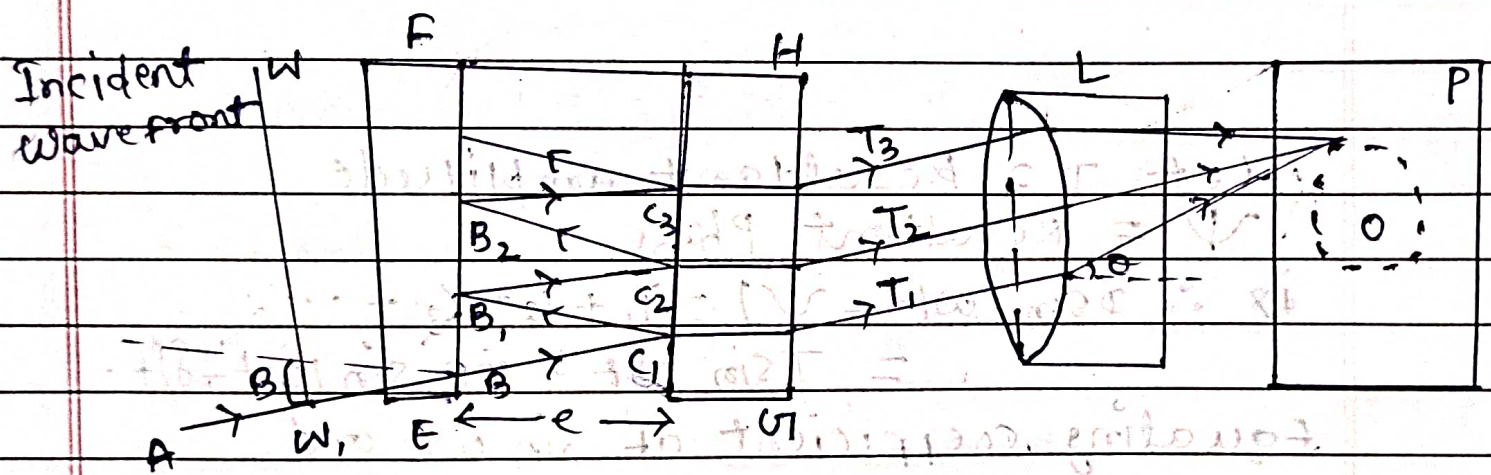


The formation of fringes in a Fabry - perot interferometer $\rightarrow$ Fabry - perot interferometer consists of two parallel high quality glass plates having silver coating in their inner surfaces. Let a monochromatic plane polarised light ray AB be incident on glass plate EF. The amplitude of light wave is one. After partial reflections and refractions between two plates, parallel rays $C_1 T_1, C_2 T_2, C_3 T_3 \dots$ emerge. These rays are coherent and are brought to focus at P on the focal plane of the lens L.



Let, T = Intensity coefficient of emergent ray
 R = Intensity coefficient of reflected ray.

Thus their amplitude coefficients will be $\sqrt{T}$ and $\sqrt{R}$ respectively. Since amplitude of incident ray is one hence amplitude of $B C_1$ is $\sqrt{T}$ for $C_1 T_1$ is T , for $B_1 C_2$ is $R\sqrt{T}$, for $C_2 T_2$ is TR and so on.

Thus phase difference between two consecutive emergent rays will be —

$$\delta = \frac{2\pi}{\lambda} \cdot 2e \cos \theta \quad (\text{Fig. - 1})$$

Let incident ray AB is represented by —

$$Y = \sin \omega t \quad [\text{Amplitude} = 1]$$

Hence emergent rays are represented by

$$Y_1 = T \sin \omega t$$

$$Y_2 = TR \sin (\omega t - \delta)$$

$$Y_3 = TR^2 \sin (\omega t - 2\delta)$$

$$\dots$$

Let $D \equiv$ Resultant amplitude

$\psi \equiv$ Resultant phase

$$\therefore D \sin (\omega t - \psi) = Y_1 + Y_2 + Y_3 + \dots$$

$$= T \sin \omega t + TR \sin (\omega t - \delta) + \dots$$

Equating coefficient of $\sin \omega t$ and $\cos \omega t$ on both sides —

$$D \cos \psi = T + TR \cos \delta + TR^2 \cos 2\delta + \dots$$

$$D \sin \psi = TR \sin \delta + TR^2 \sin 2\delta + \dots$$

$\therefore$ Resultant amplitude,

$$I \equiv D^2 = (D \cos \psi + i D \sin \psi)(D \cos \psi - i D \sin \psi)$$

where $i \equiv \sqrt{-1}$

$$\text{Here, } D \cos \psi + i D \sin \psi = T(1 + R e^{i\delta} + R^2 e^{2i\delta} + \dots)$$

$$= \frac{T}{1 - R e^{-i\delta}}$$

$$\text{and } D \cos \psi - i D \sin \psi = T(1 + R e^{-i\delta} + R^2 e^{-2i\delta} + \dots)$$

$$= \frac{T}{1 - R e^{i\delta}}$$

$$\begin{aligned}
 \therefore I &= \frac{T^2}{(1-R^2 e^{i\delta})(1-R^2 e^{-i\delta})} = \frac{T^2}{1 + R^2 - 2R \cos \delta} \\
 &= \frac{T^2}{(1-R)^2 + 4R \sin^2 \frac{\delta}{2}} = \frac{T^2}{(1-R^2) \left[1 + \frac{4R}{(1-R)^2} \sin^2 \frac{\delta}{2} \right]} \quad \text{--- (1)}
 \end{aligned}$$

for constructive interference

$$2e \cos \theta = n\lambda$$

And for destructive interference --- (2)

$2e \cos \theta = (n + \frac{1}{2})\lambda$ where, $n = 0, 1, 2, 3, \dots$
 putting equation (2) in equation (1)

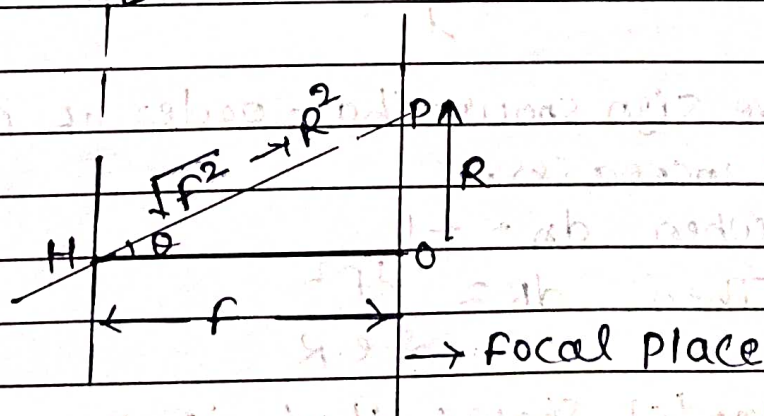
$$\text{Maximum intensity, } I_m = \frac{T^2}{(1-R)^2}$$

$$\text{Maximum intensity, } I_n = \frac{T^2}{(1+R)^2} \quad \text{--- (3)}$$

If light is not absorbed anywhere, then,

$$T = 1 - R$$

$$\therefore I_m = 1 \text{ and } I_n = \frac{(1-R)^2}{(1+R)^2}$$



Formation of fringes: Now path differences between two consecutive emergent rays,

$$2e \cos \theta = n\lambda \quad \text{--- (4)}$$

Equation (4) says that for given value of e , λ and n , the circle passing through

point p and having radius $OP = r$, has same value of θ .

Fig.-2 says that several bright concentric circular fringes having centre O will be formed. Each bright fringe is followed by a dark fringe.

$$\text{Now, } \cos \theta = \frac{f}{\sqrt{f^2 + R^2}}$$

$f =$ Focal length of lens L , $\sim \frac{1}{2}$

$$\therefore \cos \theta = \frac{1}{\sqrt{1 + \frac{R^2}{f^2}}} = \left(1 + \frac{R^2}{f^2}\right)^{-1/2}$$

$$\approx 1 - \frac{1}{2} \frac{R^2}{f^2}$$

Now from equation (4)

$$n = \frac{2e}{\lambda} \cos \theta = \frac{2e}{\lambda} \left(1 - \frac{R^2}{2f^2}\right) \quad \dots (5)$$

Differentiating:

$$dn = \frac{2e}{\lambda} (-\sin \theta \cdot d\theta) = -\frac{2e}{\lambda} \frac{R}{f^2} \cdot dR$$

Negative sign shows that order of fringe decreases when R increases.

When, $dn = -1$

$$\text{Then, } dR = \frac{1 f^2}{2 e \cdot R}$$

Equation (6) shows that if R increase then distance between fringes decreases. For large value of the distances between fringes is large.